

## Math 107H Practice Problems for Exam 2

**Show all work.** How you get your answer is just as important, if not more important, than the answer itself.

**1.** Find the volume of the region obtained by revolving the region under the graph of  $f(x) = \sin x$  from  $x = 0$  to  $x = \pi$  around the  $y$ -axis.

**2.** Find the improper integral  $\int_2^\infty \frac{1}{x(\ln x)^3} dx$ .

**3.** Determine the convergence or divergence of the following sequences:

$$(a) a_n = \frac{n^3 + 6n^2 \ln n - 1}{2 - 3n^3}$$

$$(b) b_n = \frac{n^{n+\frac{1}{n}}}{(n+3)^n}$$

**4.** Determine the convergence or divergence of the following series:

$$(a) \sum_{n=2}^{\infty} \frac{1}{(n-1)(\ln n)^{2/3}} \quad [\text{Hint: limit compare, then integral...}]$$

$$(b) \sum_{n=0}^{\infty} \frac{6n}{(1-n^2)^2}$$

**5.** Determine the convergence or divergence of the following series:

$$(a) \sum_{n=1}^{\infty} \frac{(n-1)!}{2^n n^3} \quad (b) \sum_{n=0}^{\infty} \frac{n 2^{2n+1}}{9^n + 1}$$

**6.** Set up, **but do not evaluate**, the integral which will compute the arclength of the graph of  $y = x\sqrt{1+x^2}$  from  $x = 0$  to  $x = 3$ .

**7.** Cesium-137, denoted  $\text{Cs}_{137}$ , is a radioactive substance with a half-life of 30 years. That is, if  $C(t)$  represents the amount of  $\text{Cs}_{137}$  in a sample after  $t$  years, then

$$C(30) = \frac{1}{2}C(0).$$

If we start with a 4 gram sample of  $\text{Cs}_{137}$ , how much  $\text{Cs}_{137}$  will remain after 10 years?

**8.** Find the (implicit) solutions to the differential equation

$$\frac{dy}{dt} = \frac{te^{y+t}}{y}$$