Math 208, Section 3

## Practice problems for Exam 2

1. Find the integral of the function f(x, y) = x over the region R lying between the graphs of the curves

 $y = x - x^2$  and y = x - 1 (see figure).

2. Find the integral of the function f(x, y, z) = z over the region S bounded by the planes

$$x = 0, x = y, y = 1, z = 0$$
 and

the surface 
$$z = x^2 + 1$$
 (see figure)

4. Find the critical points of the function

$$f(x,y) = x^2 - y^3 + 6xy$$

Describe what the Second Derivative Test says about each critical point.

5. (15 pts.) Calculate the first and second partial derivatives of the function  $\frac{\sin(x+y)}{\sin(x+y)}$ 

$$\frac{\ln(x+y)}{y}$$

1. (25 pts.) Find the critical points of the function  $f(x,y) = x^2 - xy^2 - 4x$ 

and determine which of rel max, rel min, or saddle point, each is.

2. (20 pts.) Find the maximum value of the function

subject to the constraint f(x, y) = x + 2y $g(x, y) = x^2 + 2y^2 = 5$ .

5. Evaluate the following double integrals (10 pts. each):

(a): 
$$\int_{0}^{1} \int_{1}^{2} x^{2}y - y^{2}x \, dx \, dy$$
  
(b):  $\int_{0}^{1} \int_{\sqrt{x}}^{1} x\sqrt{y} \, dy \, dx$ 

**5.** (20 pts.) Evaluate the integral

$$\int_{0}^{1} \int_{0}^{(1-y^3)^{1/3}} y(1-x^3)^{1/3} \, \mathrm{d}x \mathrm{d}y$$

by changing the order of integration. (Trust me, you **can't** evaluate it in the order in which it is given!)

2. (20 pts.) Find the local extrema of the function

$$f(x,y) = x^4 - 4xy + y^2 \, ,$$

and determine, for each, if it is a local max. local min, or saddle point.

3. (20 pts.) Find the maximum and minimum values of the function  $f(x,y) = 2x^2 - y + y^2$ 

subject to the constraint

$$g(x,y) = 4x^2 + y^2 \le 4$$

4. (20 pts.) Evaluate the interated integral  $\int_0^2 \int_x^2 x^2 (y^4+1)^{1/3} \ dy \ dx$ 

by rewriting the integral to reverse the order of integration.

(Note: the integral *cannot* be evaluated in the order given....)