

**Math 208, Section 3**

**Exam 1**

1. (20 pts.) Find the equation of the plane in 3-space which passes through the three points

$$(1, -1, 2), (1, 0, 1), \text{ and } (-2, 3, 5)$$

Does the point  $(1, 2, 9)$  lie on this plane??

2. (20 pts.) Find the partial derivatives of the following functions:

(a)  $f(x, y, z) = x^2y^7 - 3yz^3 + \cos(x - y)$

(b)  $g(x, y) = \frac{xy - 3y + 2}{(x + y)^2 - y^3}$

- 3.** (20 pts.) Find the equation of the tangent plane to the graph of the function

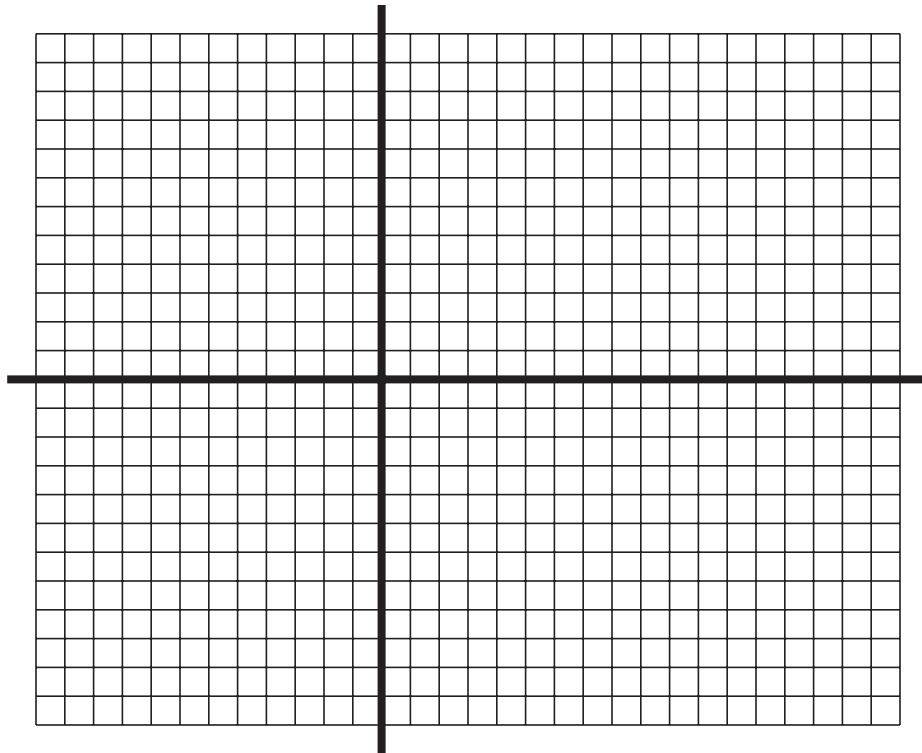
$$z = g(u, v) = 3u^2 - uv^2 + v^5$$

at the point  $(2, 1, 11)$  .

4. (20 pts.) Sketch the level curves of the function

$$z = f(x, y) = xy - 2x$$

for  $z$ -values 0, 1, 2, and -1 . (Hint: solve for  $y$  ....) Be sure to label everything appropriately.



5. Find the derivatives of the function

$$f(x, y, z) = x^2z - xy^3 + 2yz^2$$

at the point  $(1, 0, -1)$ , in the directions of the vectors

$$\vec{v} = (1, 1, 2) \quad \text{and} \quad \vec{w} = (2, -1, 1)$$

In what direction is the function  $f$  **decreasing** the fastest, at the point  $(1, 0, -1)$  ??