Math 445 Homework 1

Due Wednesday, Sept. 10

- 1. (NZM, Problem 1.3.27) Show that if n is not prime, then n|(n-1)!.
- 2. (NZM, Problem 1.3.31) Show that if f(x) is a non-constant polynomial with integer coefficients, then f(n) cannot be prime for every $n \in \mathbb{N}$. (Hint: If f(n) = p is prime, show that for every $k \in \mathbb{N}$ we have p|f(n + kp); eventually f(n + kp) is too big to be p ...)
- 3. (NZM, Problem 1.3.33) Show that for n > 1, $n^4 + n^2 + 1$ is *never* prime. (Hint: $f(x) = x^4 + x^2 + 1$ can be expressed as a product of quadratics; find the factorization!)
- 4. Show that if $2^n 1$ is prime, then n must be prime.