Math 445 Homework 4

Due Friday, October 3

- 13. Show that if n|m, and (10, m) = 1, then the period of the decimal expansion of 1/n divides the period of the decimal expansion of 1/m.
- 14. Show that for every $n \geq 2$, $\operatorname{ord}_{3^n}(10) = 3^{n-2}$. (Hint: induction! This is not entirely unlike what we did for 7^n) [N.B.: Consequently, the period of the decimal expansion of $1/3^n$ is 3^{n-2} .]
- 15. Show that if (3, n) = 1 (and (10, n) = 1), then $\operatorname{ord}_n(10) = \operatorname{ord}_{3n}(10) = \operatorname{ord}_{9n}(10)$.
- 16. Find the primitive roots of 1 mod 31. (I.e., find all $a, 1 \le a \le 31$, with $\operatorname{ord}_{31}(a) = 30$. (Hint: find one; then use one of our results to quickly find the others.)